

# Leakage Resilient Value Comparison With Application to Message Authentication

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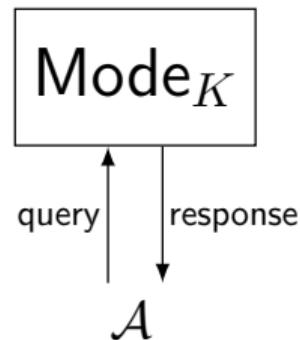
<sup>3</sup>: Radboud University (The Netherlands)



EUROCRYPT 2021

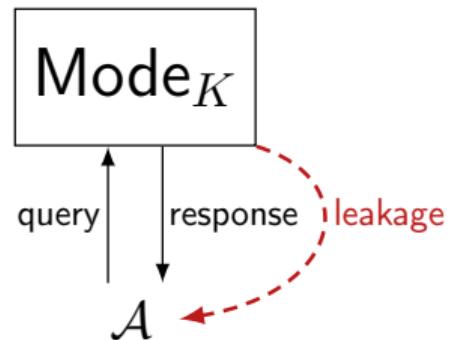
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# Black-Box Security and Side-Channel Attacks



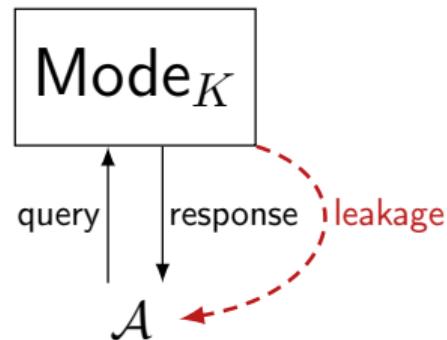
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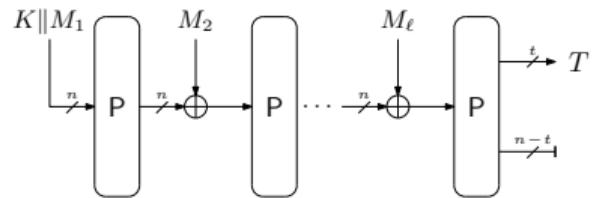
# Black-Box Security and Side-Channel Attacks



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- However, evaluations may **leak** secret information
- Two main types of countermeasures:
  - Protection at **implementation-level**: masking or hiding
  - Protection at **mode-level**: leakage resilience

## Example: Message Authentication (1/2)

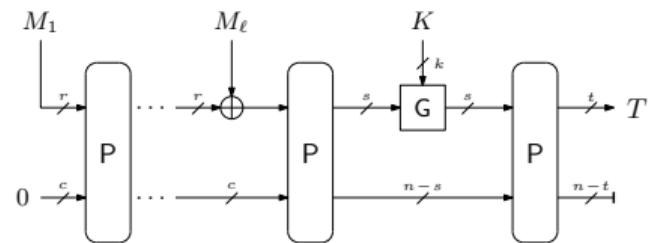
### FKS: Full-state Keyed Sponge (Simplified) [BDPV12,GPT15,MRV15]



- Very efficient
- No mode-level protection against side-channel attacks
- Requires implementation-level protection

## Example: Message Authentication (2/2)

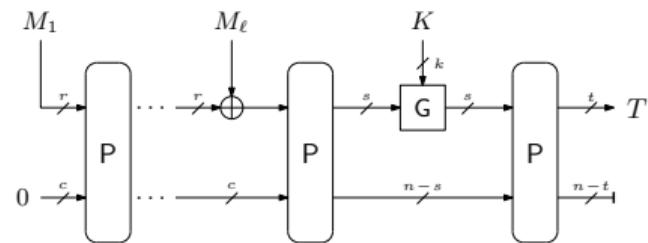
### SuKS: Suffix Keyed Sponge [BDPV11,DEM+17,DM19]



- Processes key **at the end**
- Minimizes number of evaluations of secret states
- **Leakage resilient** if  $G$  and  $P$  leak up to  $\lambda$  bits of secrecy (per evaluation)

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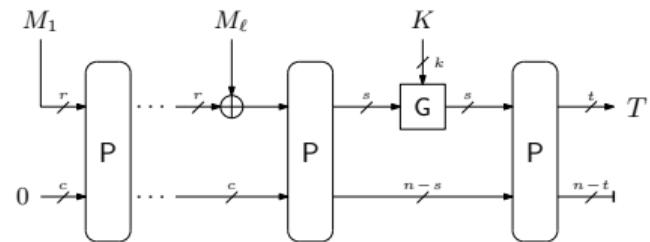


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How does SuKS verify tags?

# Closer Look at SuKS

## SuKS: Suffix Keyed Sponge [BDPV11,DEM+17,DM19]

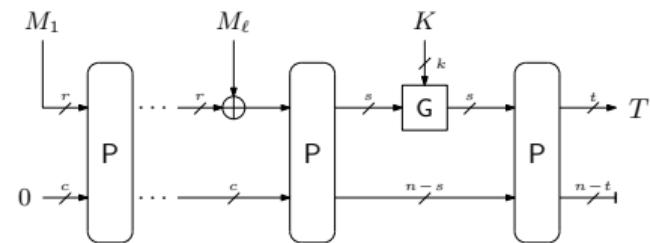


## Tag Verification

- Given message/tag tuple  $(M, T^*)$ :
  - Compute  $T = \text{SuKS}(K, M)$
  - If  $T^* = T$  return 1, otherwise return 0

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## SuKS: Suffix Keyed Sponge [BDPV11,DEM+17,DM19]



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- Given message/tag tuple  $(M, T^*)$ :
  - Compute  $T = \text{SuKS}(K, M)$
  - If  $T^* = T$  return 1, otherwise return 0
- Verification **might leak** information about  $T$ !

## Leakage from Value Comparison

- Leakage resilience usually centers around MAC/AE design
- Tag verification often left out of scope
- Assumed to be protected at implementation level

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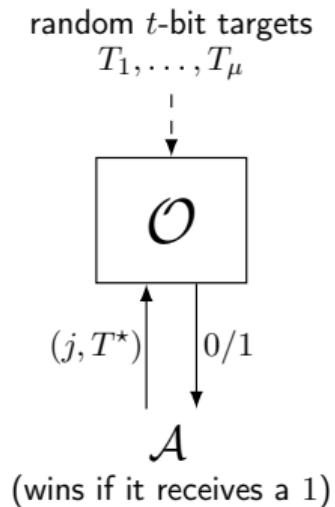
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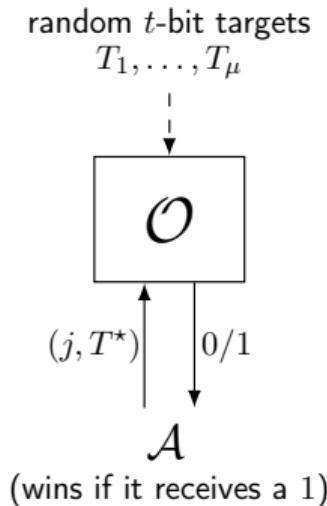
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Formal analysis of leakage resilient value comparison

## Modeling Value Comparison: Black-Box



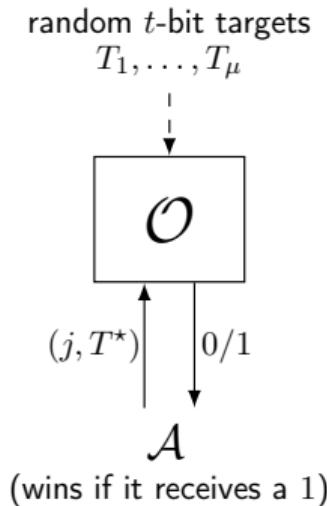
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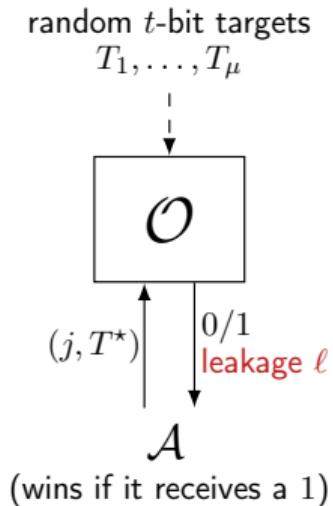
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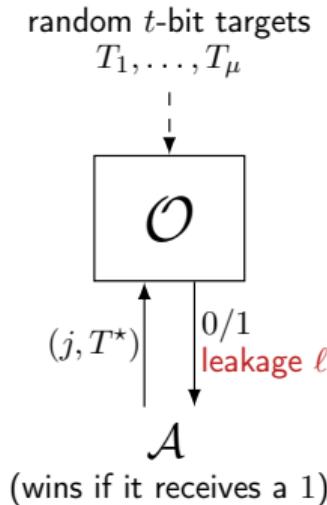
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- Adversary making  $q$  queries  
wins with probability at most  $q/2^t$

## Modeling Value Comparison: Leaky Setting



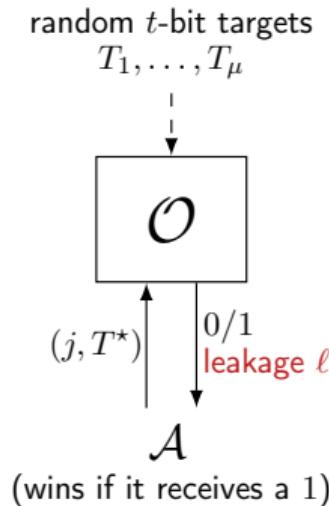
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- Plain target verification **fails**:  
 $\mathcal{O} : (j, T^*) \mapsto \left[ \left[ T_j = ? T^* \right] \right]$ 
  - Oracle might leak  $\lambda$  bits of  $T_j$  per query
  - $T_j$  is obtained after  $\lceil t/\lambda \rceil$  queries

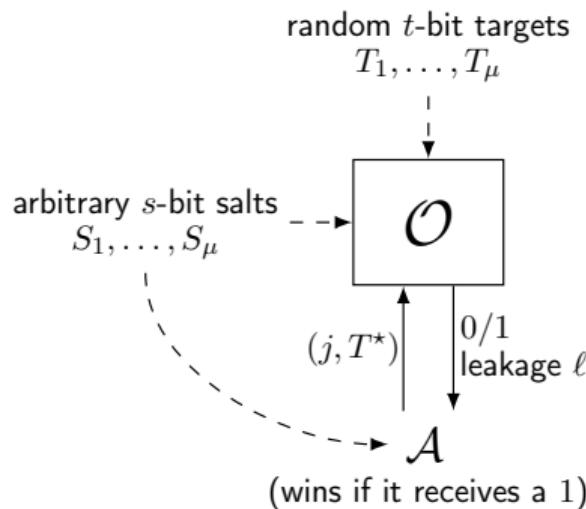
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- A **more sophisticated** oracle  $\mathcal{O}$  needed!

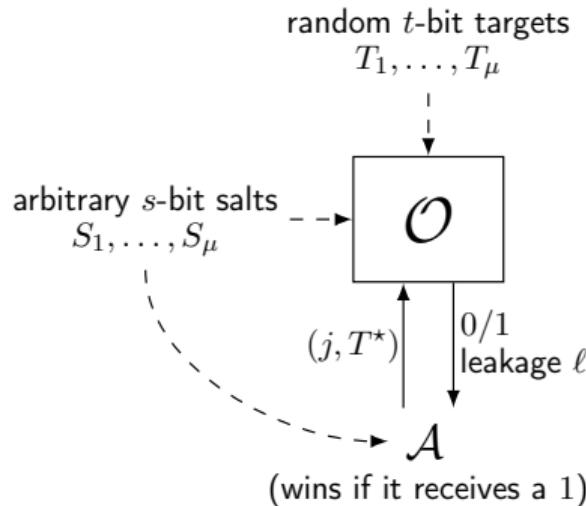
# Modeling Value Comparison: General Model

## General Model



- $\mu$  random target values  $T_1, \dots, T_\mu$
- $\mu$  salts  $S_1, \dots, S_\mu$ 
  - In principle unique
  - Randomization or omission possible
  - In applications, salts are often present

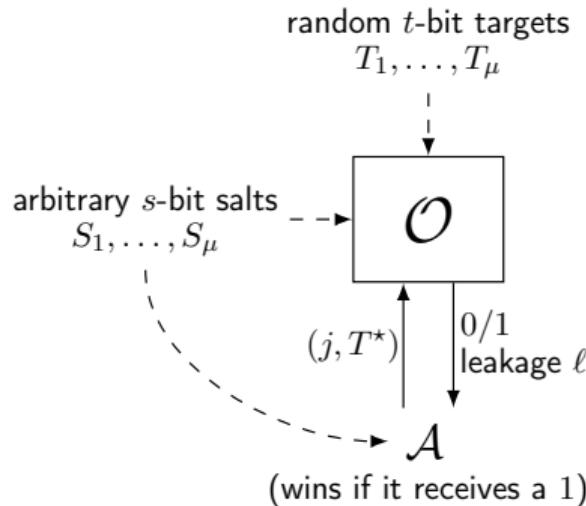
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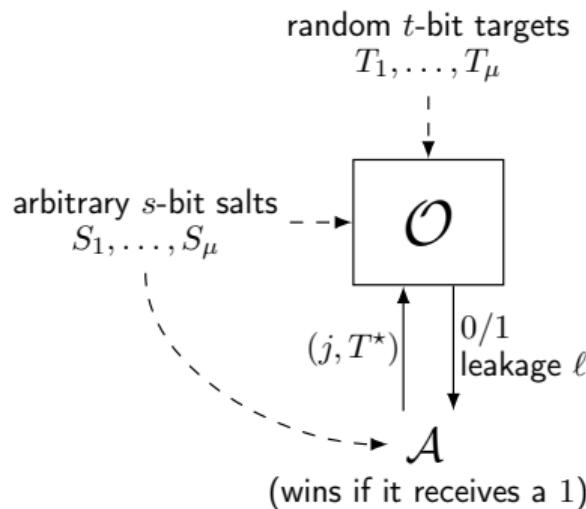
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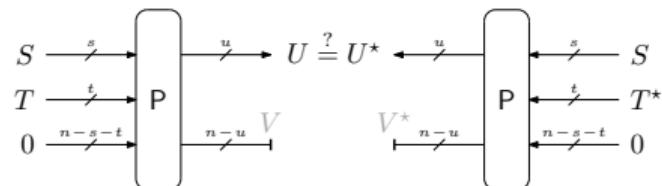
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- $\mathcal{O}$  is some verification oracle
- Adversary  $\mathcal{A}$  can make attempts  $(j, T^*) \mapsto 0/1$
- $\mathcal{A}$  also obtains leakage:
  - Evaluation of cryptographic primitive within  $\mathcal{O}$  may leak  $\lambda$  bits (non-adaptively)
  - Each value comparison may leak  $\lambda$  bits (non-adaptively)

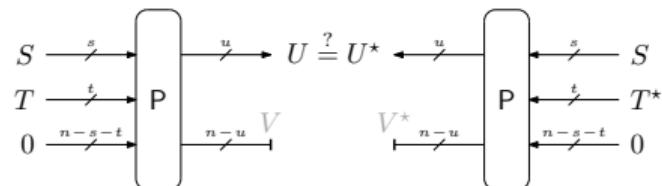
## PVP: Permutation-Based Value Processing (1/2)



- Let  $P$  be an  $n$ -bit permutation
- Consider value comparison

$$\mathcal{O} : (j, T^*) \mapsto \left[ \left[ \text{left}_u(P(S_j \parallel T_j \parallel 0^*)) \stackrel{?}{=} \text{left}_u(P(S_j \parallel T^* \parallel 0^*)) \right] \right]$$

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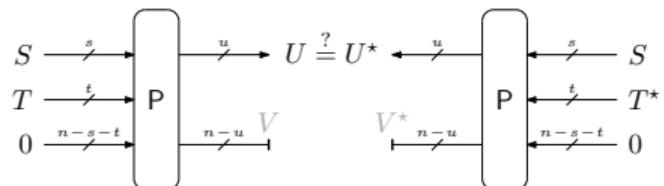


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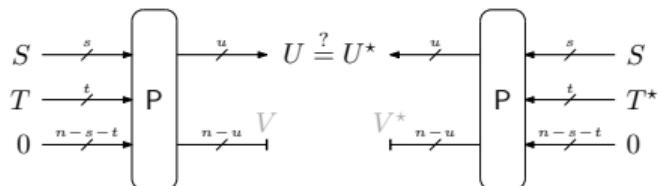
- PVP gives **leakage resilient value comparison**

## PVP: Permutation-Based Value Processing (2/2)



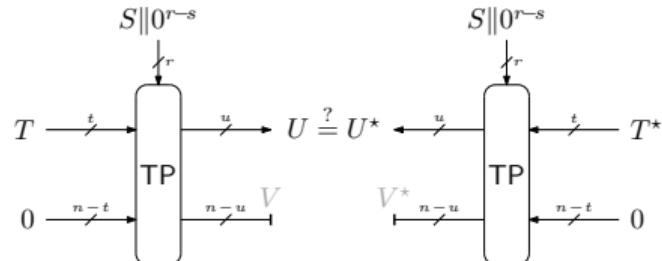
- If  $P$  is a **public permutation** (e.g., Keccak- $f$ ):
  - We require  $t, u \ll n$ , but typically  $n$  is large enough
  - Similar to earlier suggestion of designers of ISAP [DEM+19]

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  - Similar to earlier suggestion of designers of ISAP [DEM+19]
- If  $P$  is a **secret permutation** (e.g.,  $\text{AES}_K$ ):
  - No limitation on  $t, u$
  - Better security bound but one needs protected  $\text{AES}_K$

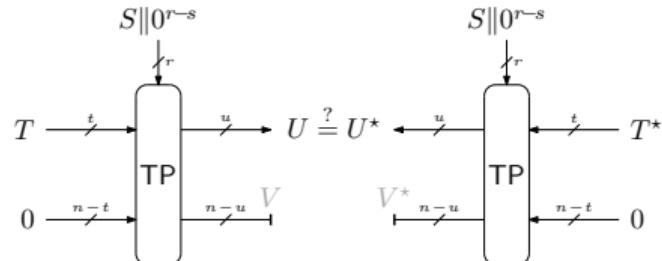
# TPVP: Tweakable Permutation-Based Value Processing



- Let TP be an  $n$ -bit tweakable permutation with  $r$ -bit tweaks
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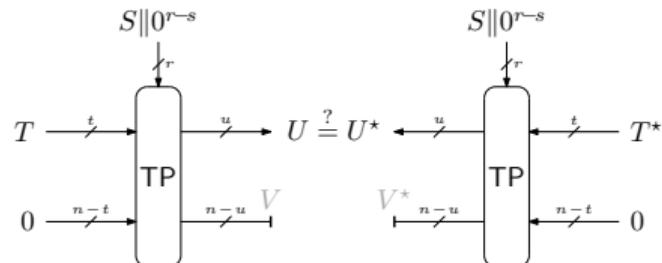


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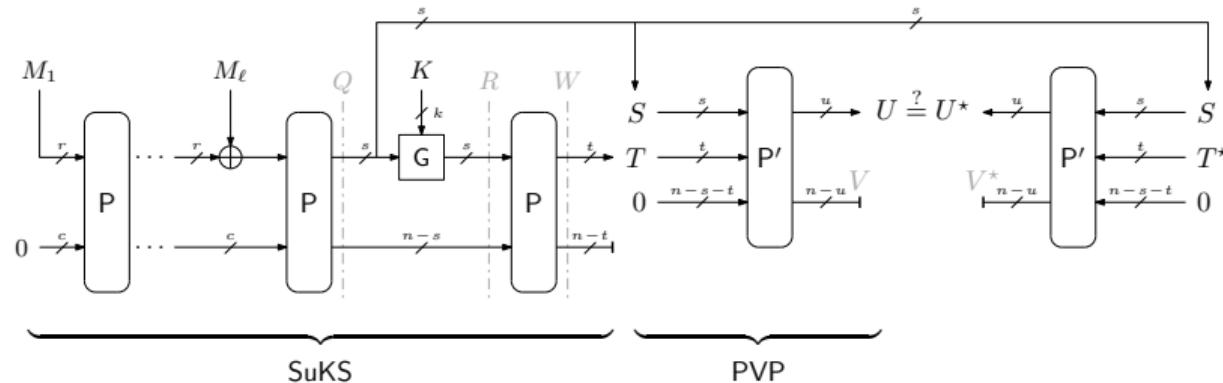


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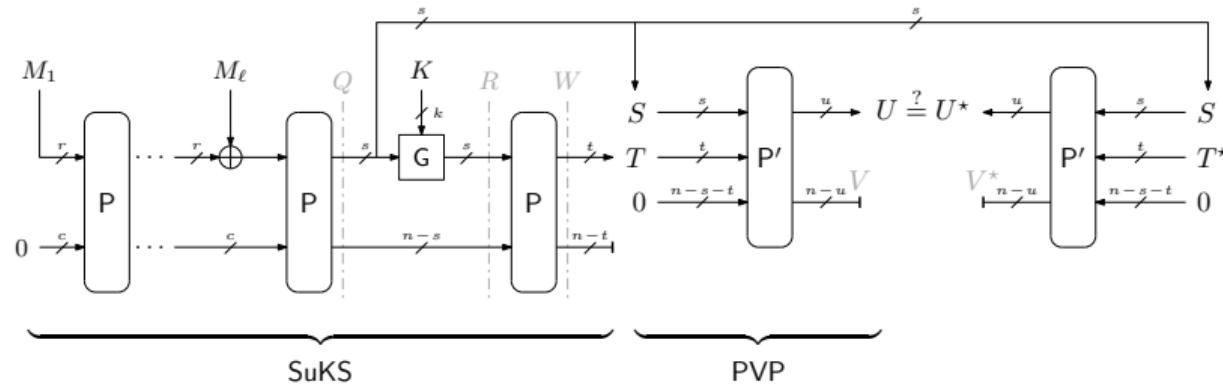
- TPVP gives **leakage resilient value comparison**
- Same conditions on  $t, u$  apply
- TPVP with secret permutation was used in Spook [BBB+19]

## SuKS-then-PVP (StP)



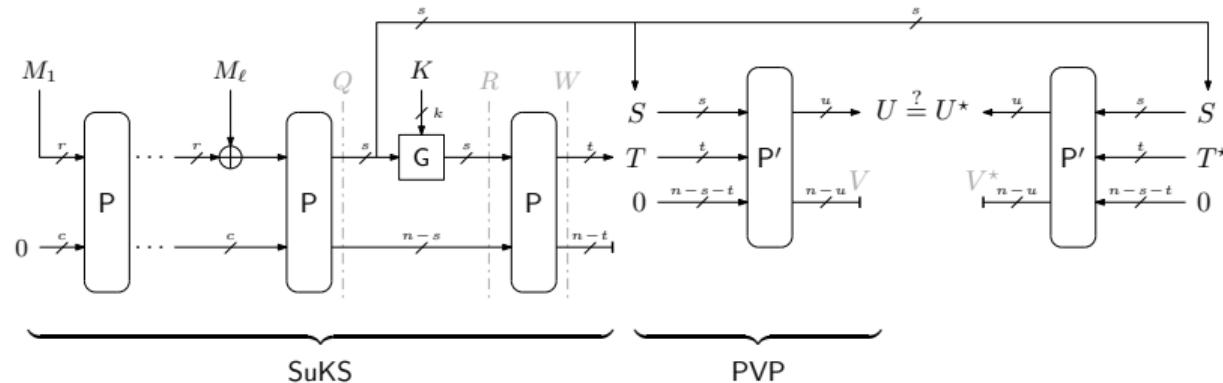
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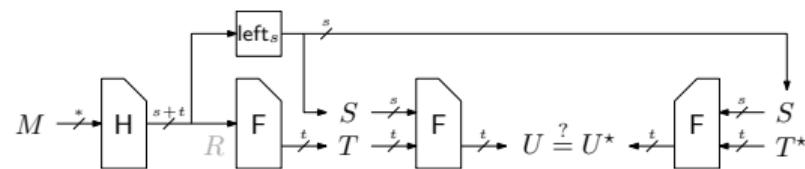
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- Disadvantage of composition: **independent** primitives P and P' needed

## Hash-then-Function-then-Function (HaFuFu)



- $H$  is hash function and  $F$  is secret random function
- HaFuFu: uses same  $F$  for MAC and for verification
- Salt taken from keyless computation of  $H$
- **Leakage resilience** of HaFuFu: as before, but dedicated proof needed

# Conclusion

## Value Comparison

- Prominent role in tag verification
- Further applications in fault countermeasures
- Can be done efficiently by re-using existing resources
- Processed value comparison leads to slightly larger success probability

## More in Paper

- Exact leakage resilience analysis
- Security assumptions
- Relaxation of salt

**Thank you for your attention!**